

## Section 1.2 Functions and their properties

**Function:** is a rule that assigns one value of the dependent variable (output/y) for each value of the independent variable (input/x). "One y for each x"

Recall vertical line test when looking at graphs

For equations pick x values to see if there is a unique output (only one answer)

**Domain:** set of input values

**Range:** set of output values

\*\*\*\*\*Give answers in interval notation!

Ex 1) Find the domain of each function

• denominator  $\neq 0$

• under  $\sqrt{\quad} \geq 0$

a)  $f(x) = \sqrt{x+3}$

$$\sqrt{x+3} \geq 0$$

$$x \geq -3$$

$$\boxed{[-3, \infty)}$$

b)  $m(x) = \frac{x}{x-5} \neq 0$

~~.....~~  
 $x \neq 5$

$$\boxed{(-\infty, 5) \cup (5, \infty)}$$

c)  $j(x) = \frac{\sqrt{x}}{x-5} \geq 0$

$$x \geq 0 \text{ and } x \neq 5$$

~~.....~~  
0                      5

$$\boxed{[0, 5) \cup (5, \infty)}$$

d)  $g(x) = \sqrt{x-16} \geq 0$

$$x \geq 16$$

$$\boxed{[16, \infty)}$$

$$e) h(x) = \frac{x}{x^2 - 4}$$

$$\frac{x}{(x-2)(x+2)}$$

$$x-2 \neq 0$$

$$x \neq 2$$

$$x+2 \neq 0$$

$$x \neq -2$$

$$(-\infty, -2) \cup (-2, 2) \cup (2, \infty)$$

$$f) c(x) = \frac{3x-1}{(x+3)(x-1)}$$

$$x+3 \neq 0$$

$$x \neq -3$$

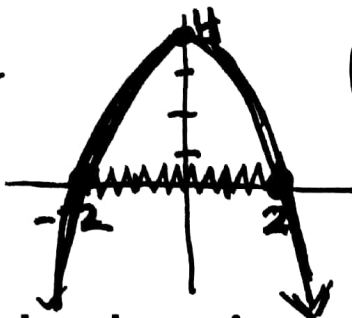
$$x-1 \neq 0$$

$$x \neq 1$$

$$(-\infty, -3) \cup (-3, 1) \cup (1, \infty)$$

$$g) k(x) = \sqrt{4-x^2} \geq 0$$

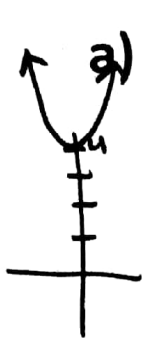
tricky quadratic under Graph Quadratic



$$[-2, 2]$$

Ex 2) Find the domain and the range of each function

(PICTURE IT!)

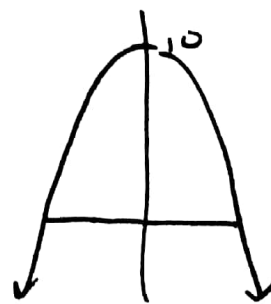


$$a) f(x) = x^2 + 4$$

$$D: (-\infty, \infty)$$

$$R: [4, \infty)$$

$$b) g(x) = 10 - x^2$$



$$D: (-\infty, \infty)$$

$$R: (-\infty, 10]$$

\*\* discuss 25,27 on HW Worksheet